

1 **Multi-Objective Resource-Constrained Scheduling in**
2 **Construction Projects**

3 Vasiliki M. Lazari and Athanasios P. Chassiakos

4 University of Patras, 26500, Patras, Greece
5 a.chassiakos@upatras.gr

6 **Abstract.** The resource-constrained scheduling problem (RCSP) is one of the
7 most challenging problems in project management. It is a combinatorial
8 optimization problem with multiple and contradictory objectives (resource
9 allocation within resource availability levels, project completion prior to a given
10 deadline, resource leveling throughout the project length) and constraints
11 (precedence constraints between activities) while its complexity grows as the
12 number of activities increases. In this study, the objective function includes a
13 number of sub-objectives that result from practical considerations of actual
14 construction projects. These are the cost of daily resources exceeding the
15 resource availability, the cost from the day by day resource movement in and
16 out of the project work, and the cost of prolonging the project duration or
17 exceeding the project completion deadline. Due to the large solution space size
18 (even for a small-sized project), genetic algorithms are employed in this study
19 to develop the optimal or a near optimal solution. The model is applied on a
20 case study project and tested for different constraints and goal scenarios, in
21 order to provide insight regarding the effectiveness of the method in different
22 optimization criteria and project management priorities. Evaluation results
23 indicate that the proposed approach can effectively approximate the optimal
24 solution in all cases.

25 **Keywords:** Resource-constrained scheduling, Resource allocation, Resource
26 leveling, Multi-objective optimization, Genetic Algorithms

27 **1 Introduction**

28 The resource-constrained scheduling problem (RCSP) has been extensively studied in
29 the past and it is still a case of great interest for researchers because of its importance
30 in project management. The aim of project scheduling analysis is to develop optimal
31 schedules with regard to time and resource allocation and leveling within resource
32 availability margins and project completion deadlines.

33 Existing research efforts have led to a variety of methods and algorithms for
34 addressing the resource-constrained scheduling problem. They can be categorized in
35 exact methods, heuristic and meta-heuristic or evolutionary algorithms. Exact
36 methods, such as linear/integer programming, attempt to tackle the problem by
37 forming mathematical relationships describing the problem objective and constraints

38 in linear form and solving with a pertinent method (e.g., Simplex method) [1-2].
39 Although these methods can provide exact solutions, they become unproductive in
40 setting up the computerized problem structure as the project size and parameters
41 increase.

42 Heuristic approaches, such as branch and bound algorithms, initially develop lists
43 of potential solutions but, because the solution space is often too vast to fully traverse,
44 they handle the problem by bounding and pruning. Main limitations of such methods
45 are that there is no universal bounding algorithm working for all problems and that
46 the optimal solution is not guaranteed. In this class of methods, the works of Brucker
47 and Knust [3] and Moukrim et al. [4] can be mentioned.

48 When the employment of previous methods is ineffective to develop or the exact
49 solution is computationally expensive to obtain, metaheuristic methods or
50 evolutionary algorithms are used in order to approximate the global optimum.
51 Evolutionary algorithms operate through the selection process in which the least fit
52 members of the population set are eliminated whereas the fit members are allowed to
53 survive and continue until better solutions are determined. Researchers have used
54 Genetic Algorithms for the exploration of near optimum solutions in resource-
55 constrained scheduling problems (Leu and Yang [5], Alcaraz et al. [6], Besikci et al.
56 [7], Kaiafa and Chassiakos [8], Mathew et al. [9]). Genetic Algorithms have also been
57 used for leveling the daily usage of resources and minimizing project duration (Roca
58 et al. [10], Ponz-Tienda et al. [11]). Other studies have combined Genetic Algorithms
59 with other evolutionary algorithms or methods to form hybrid ones so as to obtain
60 better solutions (Lova et al. [12], Bettermir and Sonmez [13]).

61 Previous studies regarding the resource-constrained scheduling problem are
62 typically based on a single (and rather theoretical) decision parameter, such as some
63 type of statistical moment of the obtained resource histogram, to evaluate the
64 effectiveness of the produced resource allocation. In this study, alternative decision
65 parameters, closer to the ones encountered in practice, are explored developing
66 different optimization structures which are comparatively evaluated to provide
67 performance indications as well as practical implications regarding the employment
68 of the alternative parameters.

69 **2 Proposed model**

70 The objective function of the proposed model represents the total cost to be
71 minimized and is formulated as the cost summation of all optimization sub-objectives.
72 The sub-objectives are the project completion goal within a deadline (or as soon as
73 possible), the confinement of the daily resource usage within the availability level,
74 and the development of a flat daily resource usage pattern throughout project
75 execution. Unit cost values are used in order to indicate the weight of each sub-
76 objective in this multi-objective formulation. More specifically, the total cost
77 (objective function) consists of the following elements:

- 78 • The project direct cost which represents the cost of the required resources for
79 project execution. This cost is proportional to the resource-days needed to
80 complete the project under normal execution and is invariant to different solutions.
81 • The indirect cost which represents the general project expenses. It is practically
82 considered to be proportional to the project duration.
83 • The cost of exceeding a given project completion deadline which represents the
84 financial impact of delaying the project beyond a specified time frame.
85 • The cost of exceeding the daily resource availability which represents the
86 (increased) expenditures needed for recruiting additional resources than initially
87 planned.
88 • The cost associated with the deviations in daily resource usage which represents
89 the cost for moving resources in and out of the construction site day by day.
90 • The cost associated with the deviations in daily resource usage which
91 (alternatively to the previous case) is considered on the basis of the standard
92 deviation of the daily resource usage histogram.

93 The above sub-objectives are considered with different unit cost values in order to
94 compare different optimization structures and criteria. For instance, if the unit cost
95 value of exceeding the daily resource availability is set at 1 while all other unit cost
96 values at 0, the optimization aims at minimizing the cumulative (along the project
97 length) number of daily resources above the resource availability level.

98 A single resource type for all activities and a single execution mode for every
99 activity (in terms of duration and daily resource usage) are considered in this study
100 and the optimization is performed by rescheduling activities according to their
101 precedence relationships and time slacks.

102 The optimization model has been implemented in an Ms-Excel spreadsheet and the
103 resource graph is automatically produced with all quantitative characteristics that
104 describe the effectiveness of the solution in accomplishing the optimization
105 objectives. The optimization is performed through genetic algorithms (GAs) via a
106 commercial optimization software (Palisade Evolver 7.5) which works as an Excel
107 add-in.

108 **3 Results**

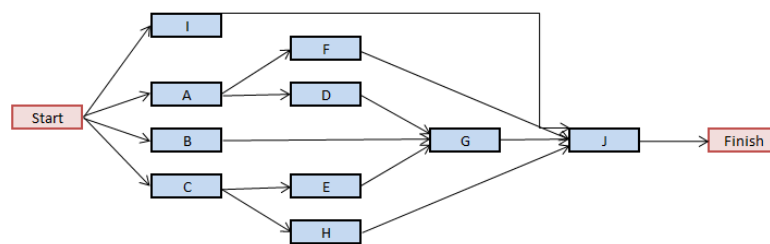
109 A case study with a simple project consisting of 10 activities is considered to illustrate
110 the algorithm application. The project activities and durations, the precedence
111 relations, and the resource requirement per activity are shown in Table 1. Figure 1
112 presents the network diagram of the project and Figure 2 the resource histogram for
113 the early project schedule (initial solution). The normal project duration is 17 days.
114 This is also considered as the desired project deadline and set as a constraint in the
115 optimization model. The resource availability level is set at 6 units per day.

116 A number of scenarios considering different optimization criteria are evaluated as
117 indicated in Table 2. Case 1 represents the initial project schedule with the earliest
118 start of the activities (Figure 2). Case 2 provides the result of minimizing the cost of
119 exceeding the daily resource availability (Figure 3). It can be seen that a considerable
120 amount of leveling has been achieved compared to the initial solution. Case 3

121 provides the result of minimizing the standard deviation of the daily resource usage.
 122 In this particular case study, the resource allocation histogram is identical to the
 123 previous one (Figure 3) and this is due to the relatively small project size that does not
 124 develop a large number of alternative resource allocation patterns. However, the
 125 experimentation with other examples shows some deviation in the final resource
 126 allocation between the two sub-objectives but this deviation is typically not enormous.
 127 In fact, the results of these two cases indicate their quite similar performance since
 128 both focus on a smooth resource histogram within the resource availability constraint.
 129 On the other hand, the optimization in Case 4 shows (rather surprisingly) that if the
 130 criterion is the minimization of the cumulative number of resources in and out of the
 131 project along its duration, the “best” histogram is not a leveled one but rather one that
 132 is leveled at different project phases. Case 5 provides an optimization result following
 133 the combination of sub-objectives of Cases 3 and 4. The resulting resource allocation
 134 histogram lies somewhere in between those produced by the individual sub-
 135 objectives.

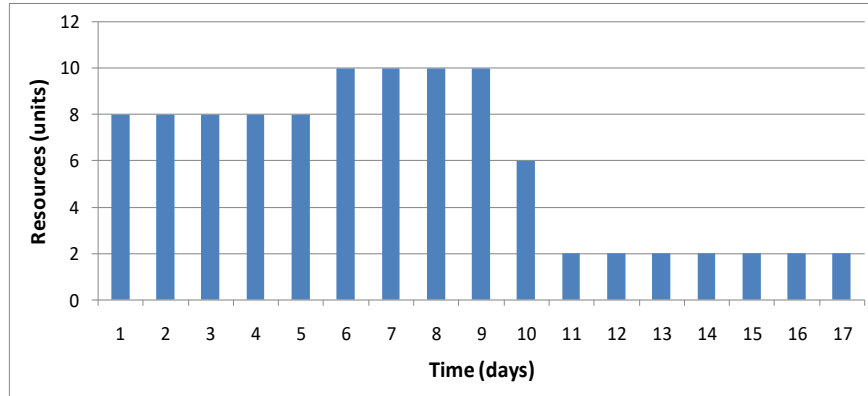
136 **Table 1.** Project data for the application example.

Activity	Predecessors	Duration	Resources
A	Start	5	2
B	Start	10	2
C	Start	4	2
D	A	7	2
E	C	5	2
F	A	4	2
G	E,D,B	3	2
H	C	6	2
I	Start	4	2
J	F,G,H,I	2	2



137
 138

Fig. 1. Network diagram of the example project



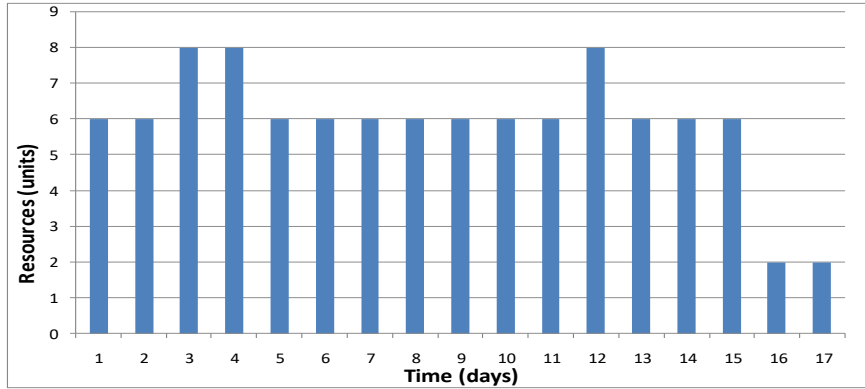
139
140

Fig. 2. Resource histogram for the early start project schedule.

141

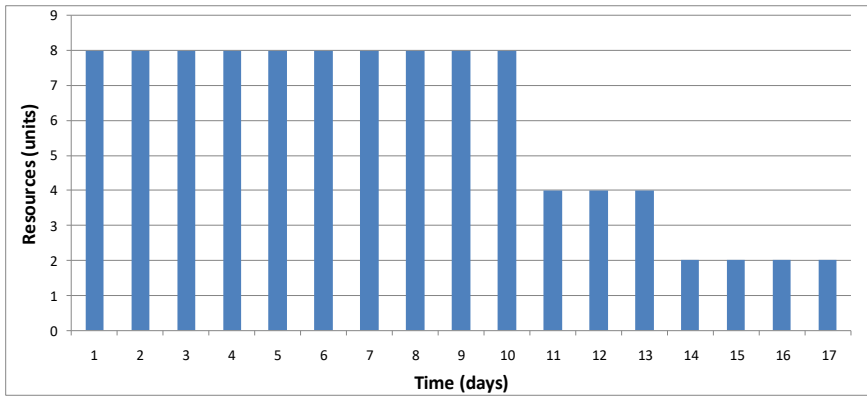
Table 2. Optimal results for example project

Case no	Case description	Resource constraint	Project duration	Resource standard deviation	Resource exceedance	Resource fluctuations
1	Initial early time schedule	-	17	4.00	26	10
2	Resource allocation under resource constraint – minimizing resource availability exceedance	$R \leq 6$	17	3.11	6	12
3	Resource allocation under resource constraint – minimizing resource standard deviation	$R \leq 6$	17	3.11	6	12
4	Resource allocation under resource constraint – minimizing resource fluctuations	$R \leq 6$	17	3.56	20	6
5	Resource allocation under resource constraint – minimizing resource standard deviation and fluctuations	$R \leq 6$	17	3.16	8	6



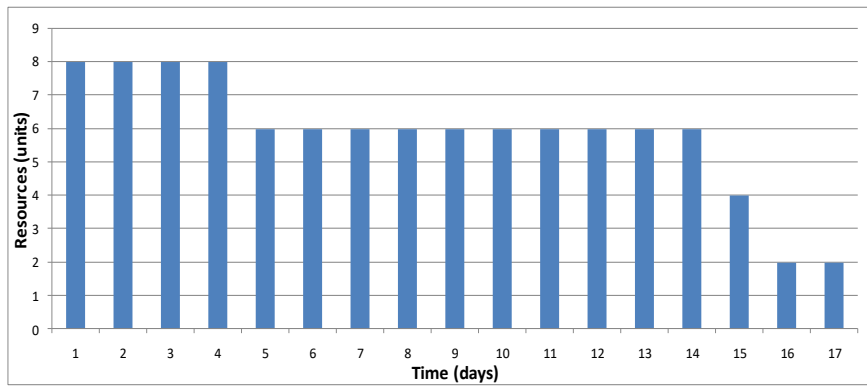
142
143

Fig. 3. Resource histogram for Cases 2 and 3.



144
145

Fig. 4. Resource histogram for Case 4.



146
147

Fig. 5. Resource histogram for Case 5.

148 **4 Discussion**

149 On the basis of the results presented in Section 3 and from further elaboration with
150 other case studies, the following observations can be made:

- 151 • The resource-constrained scheduling problem is a very complex one taking into
152 account that activities should not only be optimally shaped (resource requirement,
153 duration, placement at the right time frame) but also that there are other types of
154 constraints that need to be satisfied (activities precedence relations, resource
155 availability, completion deadline). As a result, metaheuristic algorithms seem to
156 be more appropriate for solving the problem than exact optimization methods.
- 157 • The application of genetic algorithms (or any other type of metaheuristics) to
158 solve the resource-constrained problem does not guarantee finding the optimal
159 solution in a single run of the algorithm (or ever). To improve the success rate
160 (i.e., to minimize the deviation from the optimal solution), it is suggested to run
161 the algorithm repetitively to make use of the fact that, due to the stochastic nature
162 of the algorithm, the results do not generally coincide from run to run.
- 163 • Different optimization criteria should be developed in order to find the one that
164 better fits the individual problem objectives and characteristics. Focusing solely
165 on a single sub-objective may exclude alternatives with a higher generalized
166 resource allocation impact.

167 **5 Conclusions**

168 The resource-constrained scheduling problem is one of the most challenging in the
169 area of project management. It is a combinatorial optimization problem which
170 incorporates conflicting objectives (resource allocation within resource availability
171 thresholds, project completion within certain deadlines, resource leveling) and
172 constraints (e.g., precedence relation constraints between activities) while its
173 complexity grows as the number of activities increases. The size of the solution space
174 in such cases leads to the need for employing metaheuristics to obtain an
175 approximation of the optimal solution.

176 In this work, an optimization model is developed for multi-objective resource-
177 constrained scheduling. The aim of this optimization is to minimize a cost function
178 which is composed by the sum of individual cost parameters associated with (a)
179 resource availability exceedance, (b) day-by-day resource fluctuations and (c) project
180 completion beyond a given deadline. The present study examines different objectives
181 and criteria, either separately or in combination, to evaluate the degree that each
182 optimization structure facilitates certain or prevailing objectives in actual projects.
183 The optimization is performed with the employment of genetic algorithms as an
184 effective tool to handle large combinatorial problems. The evaluation indicates that
185 the proposed method can provide reliable solutions for the multi-objective resource-
186 constrained scheduling considering the priorities and individual objectives in every
187 project case.

188 **References**

- 189 1. Shtub, A., Bard, J., Globerson, S.: Project Management: Engineering, Technology, and
190 Implementation. Prentice Hall International Editions (1994).
- 191 2. Damay, J., Quilliot, A., Sanlaville, A.: Linear programming based algorithms for
192 preemptive and non-preemptive RCPSP. *European Journal of Operational Research* 182,
193 1012–1022 (2007).
- 194 3. Brucker, P., Knust, S.: Lower Bounds for Resource-constrained Project Scheduling
195 Problems. *European Journal of Operational Research* 149, 302-313 (2003).
- 196 4. Moukrim, A., Quilliot, A., Toussaint, H.: An effective branch-and-price algorithm for the
197 Preemptive Resource Constrained Project Scheduling Problem based on minimal Interval
198 Order Enumeration. *European Journal of Operational Research* 244 (2), 360–368 (2015).
- 199 5. Leu, B.S., Yang, C.H.: GA-based multicriteria optimal model for construction scheduling.
200 *Journal of Construction Engineering and Management* 126 (6), 420–427 (1999).
- 201 6. Alcaraz, J., Maroto, C., Ruiz, R.: Solving the multi-mode resource-constrained project
202 scheduling problem with genetic algorithms. *Journal of the Operational Research Society*
203 54 (6), 614–626 (2003).
- 204 7. Besikci, U., Blige, U., Ulusoy, G.: Multi-Mode Resource Constrained Multi-Project
205 Scheduling and Resource Portfolio Problem. *European Journal of Operational Research*
206 240, 22-31 (2014).
- 207 8. Kaiafa, S. and Chassiakos, A.P.: A genetic algorithm for optimal resource-driven project
208 scheduling. *Procedia Engineering* 123, 260-267 (2015).
- 209 9. Mathew, J., Brijesh, P., Dileepal, J., Tinjumol, M.: Multi Objective Optimization for
210 Scheduling Repetitive Projects using GA. *Procedia Technology* 25, 1072 – 1079 (2016).
- 211 10. Roca, J., Pugnaghi, E., Libert, G.: Solving an extended resource leveling problem with
212 multi-objective evolutionary algorithms. *World Academy of Science, Engineering and*
213 *Technology* 46, 712–723 (2008).
- 214 11. Ponz-Tienda, H., Yepes, V., Moreno-Flores, J.: The Resource Leveling Problem with
215 multiple resources using an adaptive genetic algorithm. *Automation in Construction* 29,
216 161-172 (2013).
- 217 12. Lova, A., Tormos, P., Cervantes, M., Barber, F.: An efficient hybrid genetic algorithm for
218 scheduling projects with resource constraints and multiple execution modes. *International*
219 *Journal of Production Economics* 117 (2), 302–316 (2009).
- 220 13. Bettemir, Ö. H., Sonmez, R.: Hybrid Genetic Algorithm with Simulated Annealing for
221 Resource-Constrained Project Scheduling. *Journal Of Management In Eneering* 31 (5),
222 (2015).